

# SOLVE FRACTIONAL INEQUALITIES WITH NEGATIVES

Answer all of these questions. Remember to show your working out in all questions.

## MAIN QUESTIONS

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| 1. $\frac{1}{x} < 2$                                 | 2. $-\frac{1}{x} > 3$                                  |
| 3. $\frac{2}{(x-1)} \leq -1$                         | 4. $-\frac{3}{(x+2)} > 2$                              |
| 5. $\frac{1}{(2x)} \geq -4$                          | 6. $-\frac{2}{(3x)} < 1$                               |
| 7. $\frac{(x+1)}{(x-2)} > 0$                         | 8. $\frac{(x-3)}{(x+1)} \leq 0$                        |
| 9. $\frac{(-x+2)}{(x-4)} \geq 0$                     | 10. $\frac{(-2x+1)}{(x+3)} < 0$                        |
| 11. $\frac{3}{(x-1)} + \frac{1}{(x+2)} > 0$          | 12. $\frac{2}{(x+1)} - \frac{1}{(x-3)} \leq 0$         |
| 13. $\frac{(x^2-4)}{(x+3)} > 0$                      | 14. $\frac{(x^2-9)}{(x-1)} \leq 0$                     |
| 15. $\frac{(-x^2+1)}{(x+2)} \geq 0$                  | 16. $\frac{(2x-1)}{(x^2-4)} < 0$                       |
| 17. $\frac{(x+3)}{(x^2-1)} \geq 0$                   | 18. $\frac{(-x-2)}{(x^2-9)} > 0$                       |
| 19. $\frac{1}{(x-2)} + \frac{2}{(x+1)} < 1$          | 20. $\frac{3}{(x+2)} - \frac{1}{(x-1)} \geq 2$         |
| 21. $\frac{(2x+1)}{(x-3)} - \frac{(x-2)}{(x+1)} > 0$ | 22. $\frac{(x+4)}{(x-2)} + \frac{(x-1)}{(x+3)} \leq 1$ |
| 23. $ \frac{1}{x}  > 2$                              | 24. $ \frac{(x-1)}{(x+2)}  \leq 3$                     |
| 25. $ \frac{2}{(x-3)}  < 1$                          | 26. $ \frac{(-x+2)}{(x+1)}  \geq 2$                    |
| 27. $\frac{(x^2-1)}{(x+2)^2} > 0$                    | 28. $\frac{(x-3)^2}{(x+1)} \leq 0$                     |

29.  $(-x^2+4)/(x-1)^2 \geq 0$

30.  $(2x+1)^2/(x^2-4) < 0$

## MASTER QUESTIONS



- M1.** A chemical reaction rate  $R$  is given by  $R = k/(T+273)$  where  $k$  is a constant and  $T$  is temperature in  $^{\circ}\text{C}$ . For the reaction to proceed at a rate greater than  $0.01k$ , find the temperature range.
- M2.** The efficiency  $E$  of a machine is modelled by  $E = (100-P)/(P+20)$  where  $P$  is power input in watts. Find when efficiency exceeds 50%.
- M3.** A car's fuel consumption  $C$  in litres per 100km is given by  $C = 8 + 12/(v-40)$  where  $v$  is speed in km/h. Determine speeds where consumption is less than 10 litres/100km.
- M4.** The profit  $P$  in thousands of pounds for a company is  $P = (x-50)/(x+10)$  where  $x$  is units sold in hundreds. Find when profit is negative.
- M5.** A spring's extension  $e$  in cm under load  $L$  kg is  $e = 5L/(L-2)$ . Find loads where extension exceeds 10cm.
- M6.** The concentration  $C$  of a drug in mg/litre over time  $t$  hours is  $C = 20t/(t^2-4)$ . Determine when concentration is below 2mg/litre.
- M7.** A population growth rate  $r$  is given by  $r = (N-1000)/(N+500)$  where  $N$  is population size. Find when growth rate is positive.
- M8.** The pressure  $P$  in kPa in a container is  $P = 150/(T-293)$  where  $T$  is temperature in Kelvin. Find temperatures where pressure is less than -30kPa.
- M9.** A beam's deflection  $d$  in mm under load  $w$  kg is  $d = (w^2-16)/(w-4)$ . Find loads where deflection is positive.
- M10.** The cost per unit  $C$  in pounds is  $C = (2x+10)/(x-5)$  where  $x$  is production units in thousands. Determine production levels where cost per unit is less than £3.